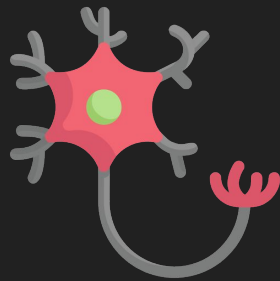
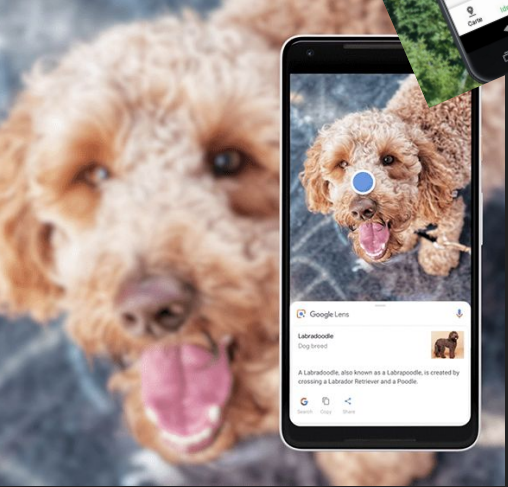
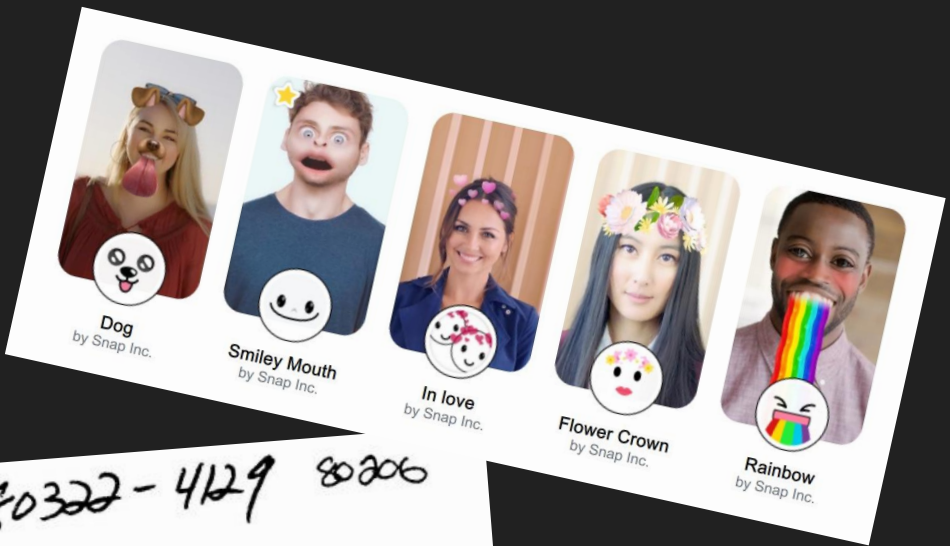
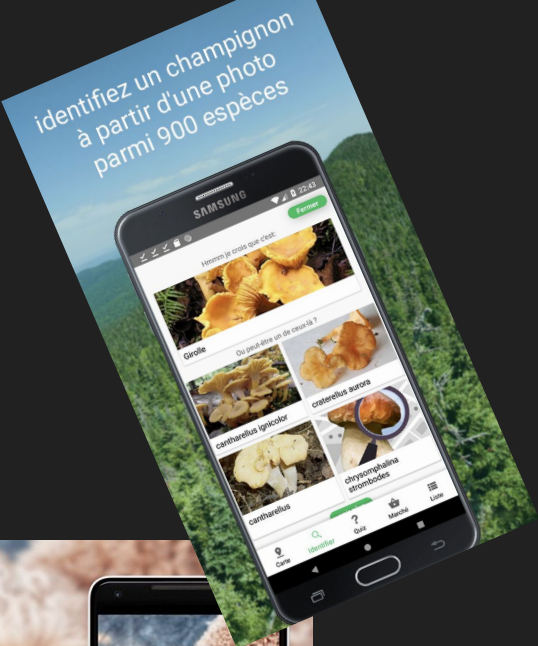
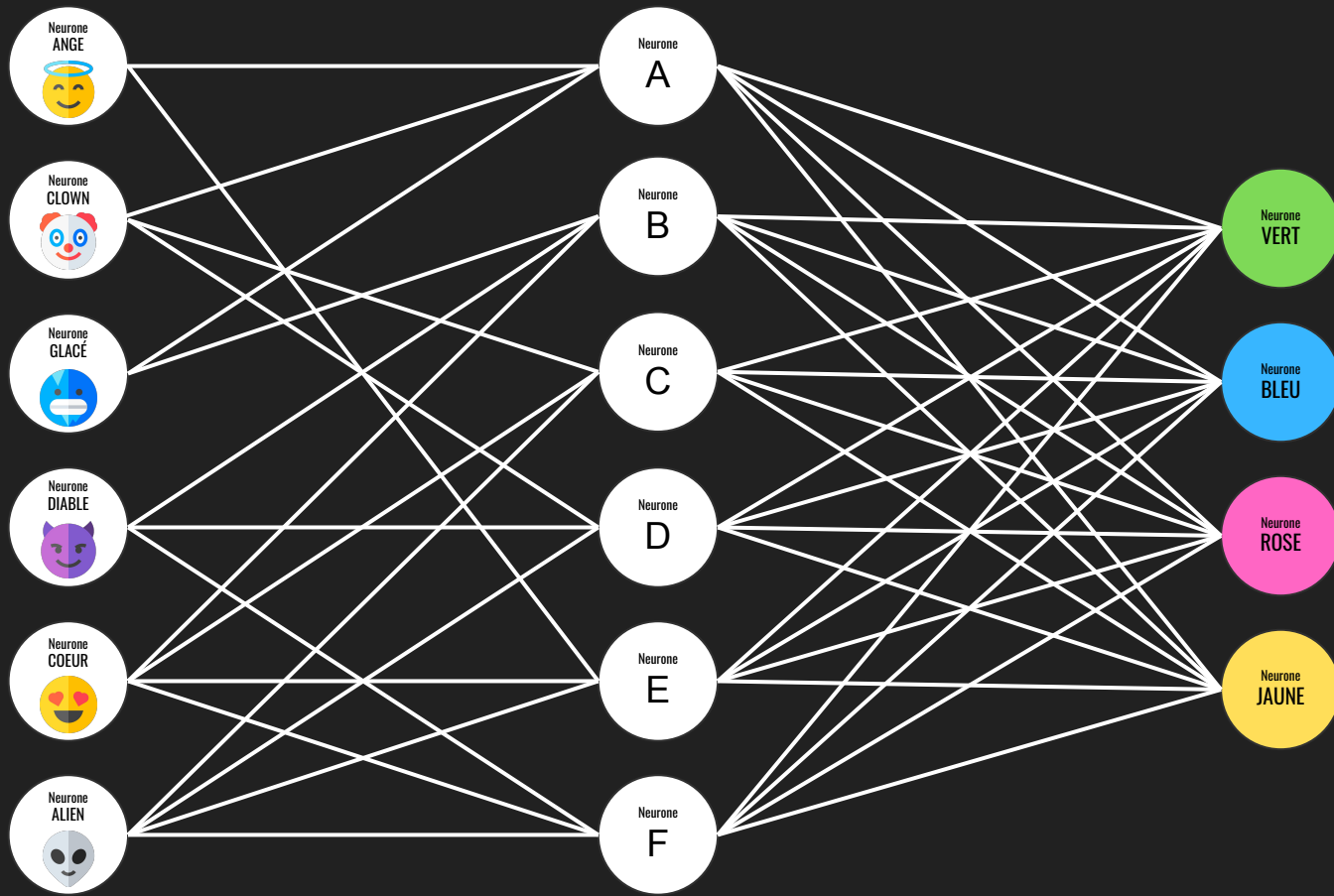


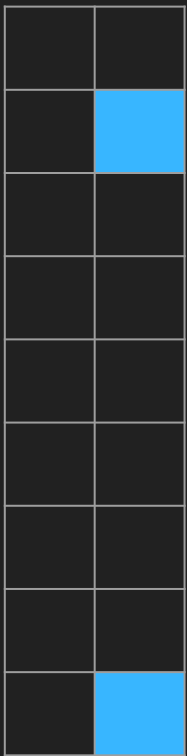
Connecte tes neurones !




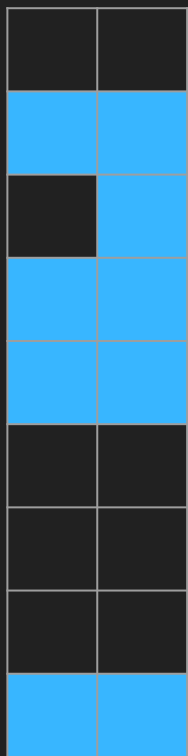



80322-4129 80206
 40004 64310
 37879 05453
 33502 75216
 35460 44209

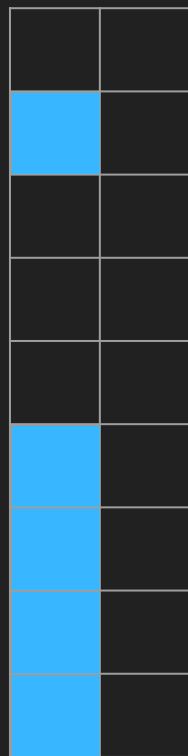






Neurone


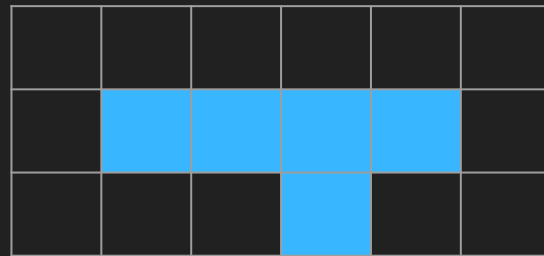



Neurone


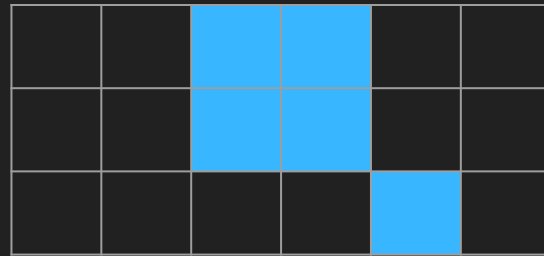



Neurone


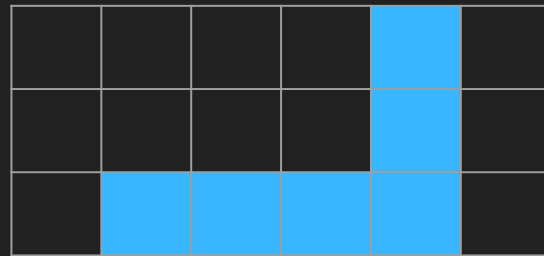
Neurone


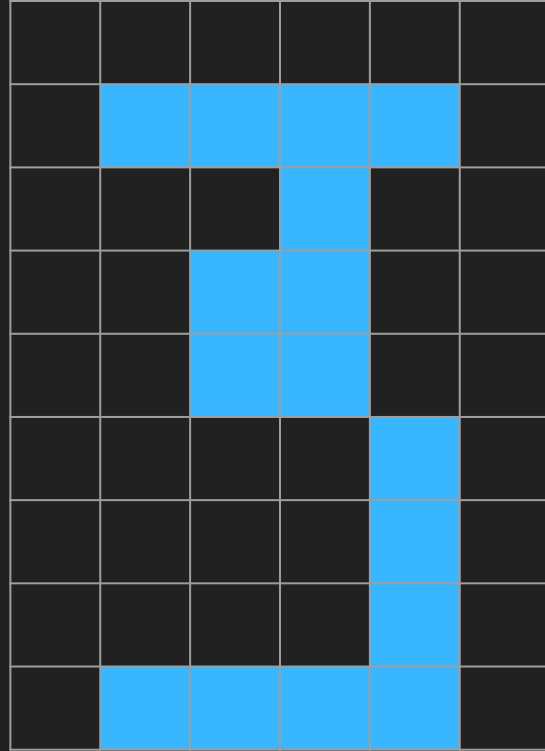


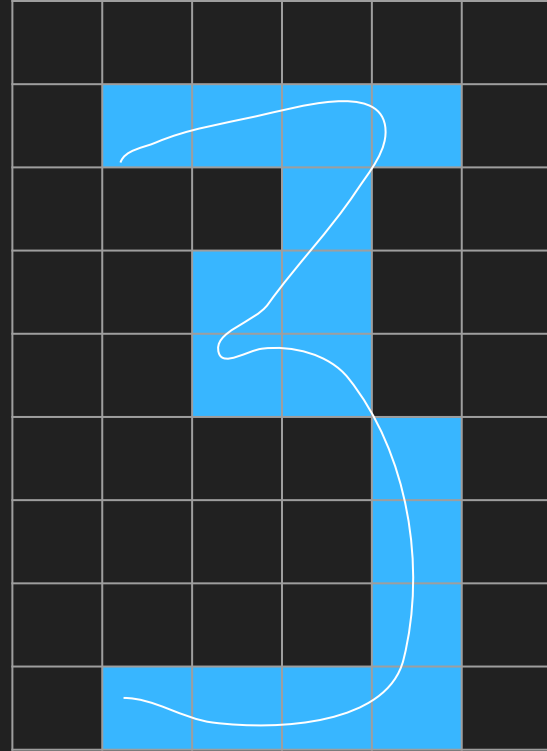
Neurone


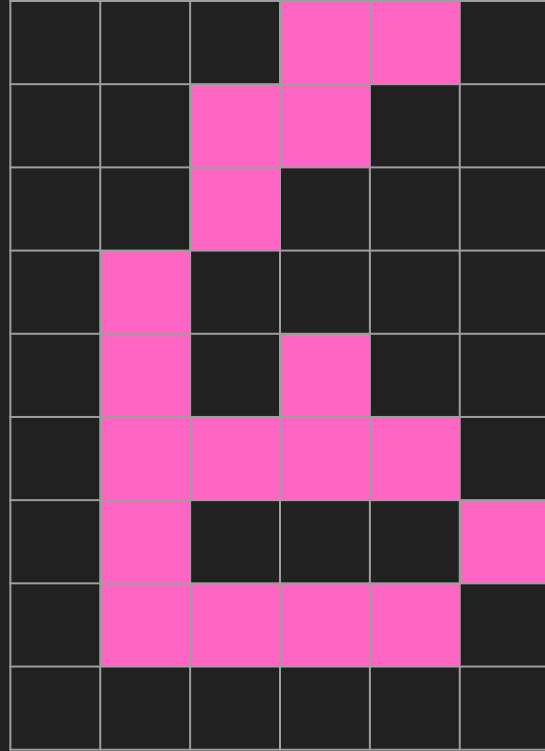


Neurone










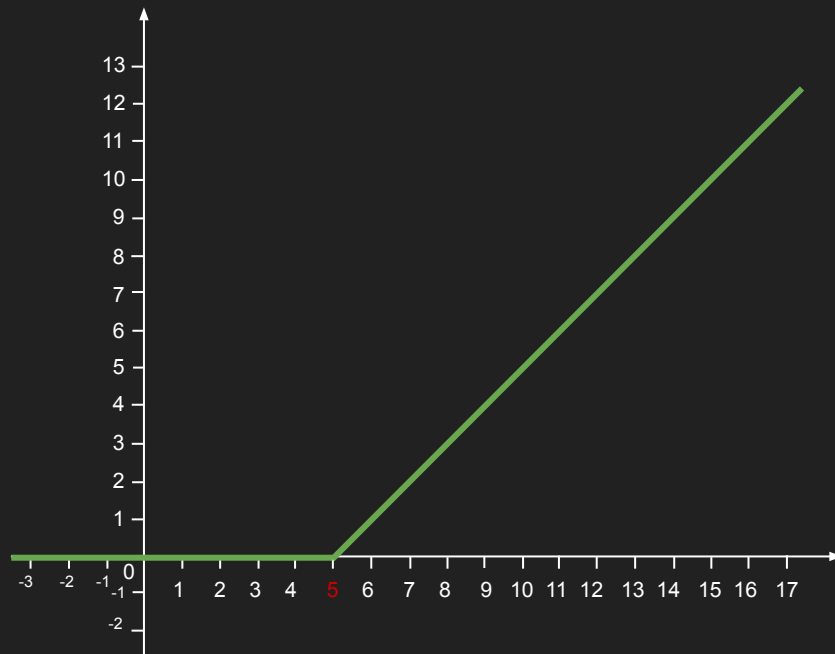
Rôle du neurone F

1 FAIS LE CALCUL SUIVANT :

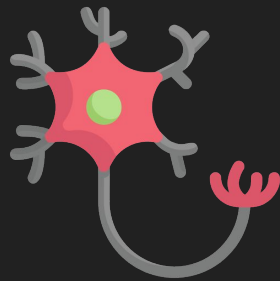
$$\text{😺} + \text{😸} - \text{😻} = ?$$

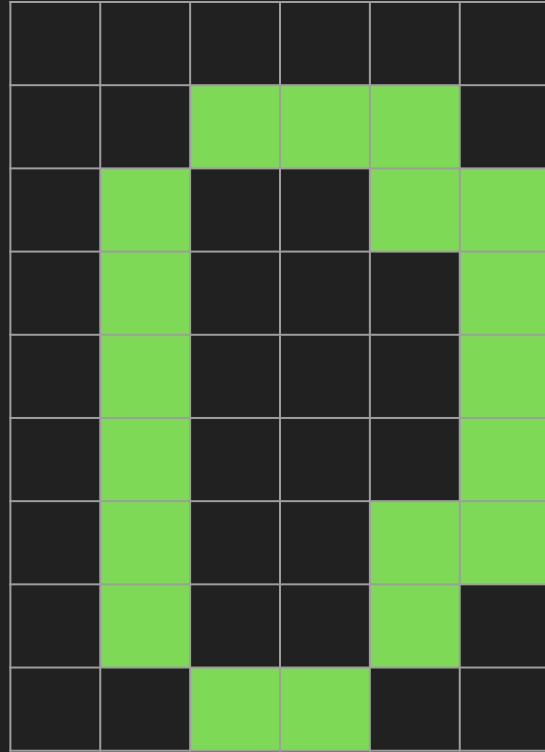
2 TROUVE LA RÉPONSE À MONTRER :

Résultat du calcul	1	2	3	4	5	6	7	8	9
$\text{😺} + \text{😸} - \text{😻}$									
Réponse à montrer	0	0	0	0	0	1	2	3	4



Connecte tes neurones !





Résultat du calcul

Sortie du
neurone

Neurone A

Neurone B

Neurone C

Neurone D

Neurone E

Neurone F

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B		
Neurone C		
Neurone D		
Neurone E		
Neurone F		

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C		
Neurone D		
Neurone E		
Neurone F		

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C	21	4
Neurone D		
Neurone E		
Neurone F		

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C	21	4
Neurone D	5	0
Neurone E		
Neurone F		

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C	21	4
Neurone D	5	0
Neurone E	19	3
Neurone F		

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C	21	4
Neurone D	5	0
Neurone E	19	3
Neurone F	7	2

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C	21	4
Neurone D	5	0
Neurone E	19	3
Neurone F	7	2

ENVOYÉ À LA COUCHE SUIVANTE

Résultat du calcul Sortie du neurone

Neurone vert

Neurone bleu

Neurone rose

Neurone jaune

Résultat du calcul

Sortie du neurone

Neurone vert

9

3

Neurone bleu

Neurone rose

Neurone jaune

Résultat du calcul Sortie du neurone

Neurone vert

9

3

Neurone bleu

- 7

0

Neurone rose

Neurone jaune

Résultat du calcul Sortie du neurone

Neurone vert	9	3
Neurone bleu	-7	0
Neurone rose	-3	0
Neurone jaune		

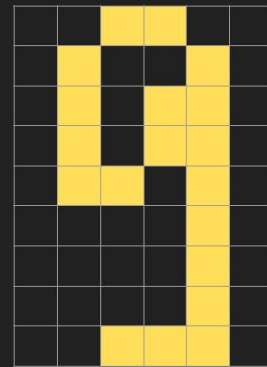
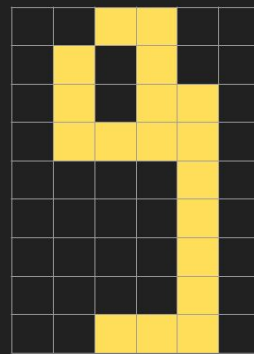
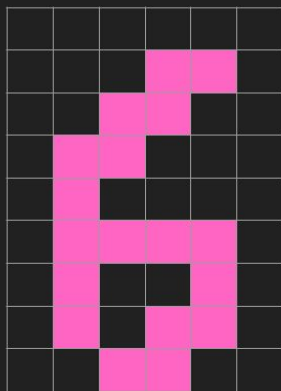
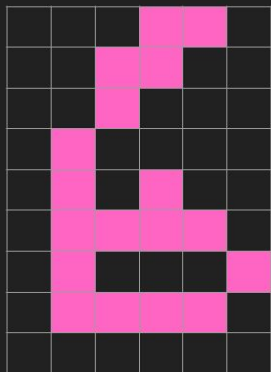
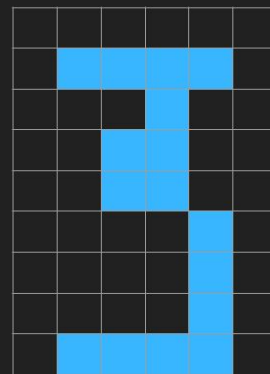
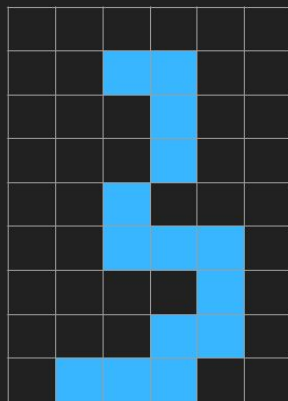
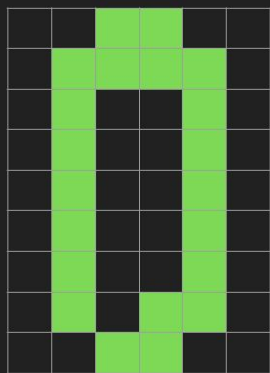
Résultat du calcul Sortie du neurone

Neurone vert	9	3
Neurone bleu	-7	0
Neurone rose	-3	0
Neurone jaune	1	0

Résultat du calcul Sortie du neurone

Neurone vert	9	3
Neurone bleu	-7	0
Neurone rose	-3	0
Neurone jaune	1	0

C'EST UN 0!



3	4	5	6	7	8	9	10	11	12	13	14	15
				0	6			9	3			
				0	6				3			
									9			
0	0	0	0	0	0	1	2	3	4	5	6	7

Neurone A

3	4	5	6	7	8	9	10	11	12	13	14	15
		0	0				3		6	3		
		9	9				6					
0	0	0	0	0	1	2	3	4	5	6	7	8

Neurone D

1	2	3	4	5	6	7	8	9	10	11	12	13
		0			0		3	3	6			
								6				
								9				
								9				
0	0	0	0	0	0	0	1	2	3	4	5	6

Neurone B

12	13	14	15	16	17	18	19	20	21	22	23	24
3	3	9		9		6	0	0				
							6					
0	0	0	0	0	1	2	3	4	5	6	7	8

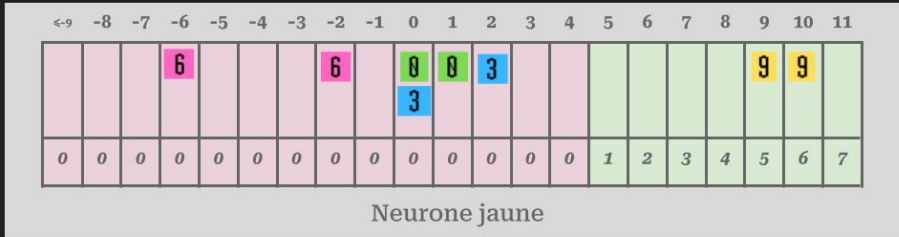
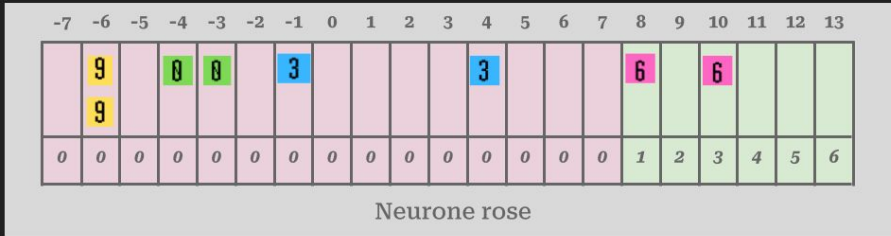
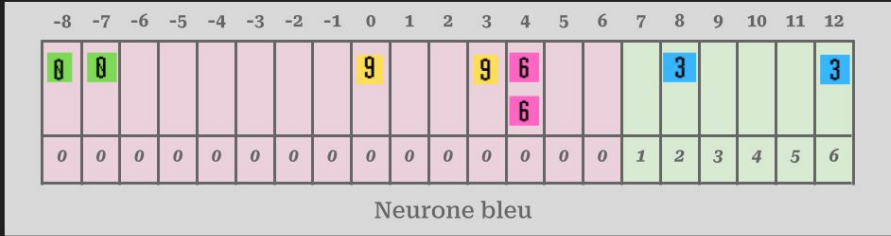
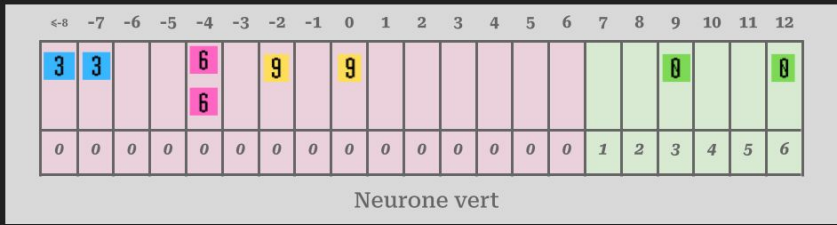
Neurone E

11	12	13	14	15	16	17	18	19	20	21	22	23
3				3	6				9	0	9	
				6						0		
0	0	0	0	0	0	0	1	2	3	4	5	6

Neurone C

0	1	2	3	4	5	6	7	8	9	10	11	12
				3	9	3	0		0			
				6								
				6		9						
0	0	0	0	0	0	1	2	3	4	5	6	7

Neurone F



3	4	5	6	7	8	9	10	11	12	13	14	15
				0	6			9	3			
				0	6				3			
									9			
0	0	0	0	0	0	1	2	3	4	5	6	7

Neurone A

3	4	5	6	7	8	9	10	11	12	13	14	15
		0	0				3		6	3		
		9	9				6					
0	0	0	0	0	1	2	3	4	5	6	7	8

Neurone D

1	2	3	4	5	6	7	8	9	10	11	12	13
		0			0		3	3	6			
								6				
								9				
								9				
0	0	0	0	0	0	0	1	2	3	4	5	6

Neurone B

12	13	14	15	16	17	18	19	20	21	22	23	24
3	3	9		9		6	0	0				
							6					
0	0	0	0	0	1	2	3	4	5	6	7	8

Neurone E

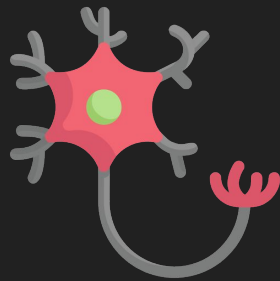
11	12	13	14	15	16	17	18	19	20	21	22	23
3				3	6				9	0	9	
				6						0		
0	0	0	0	0	0	0	1	2	3	4	5	6

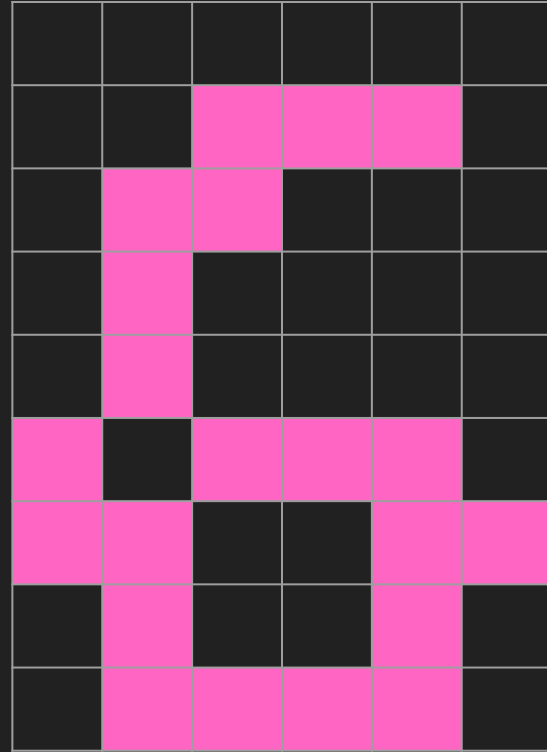
Neurone C

0	1	2	3	4	5	6	7	8	9	10	11	12
				3	9	3	0		0			
				6								
				6		9						
0	0	0	0	0	0	1	2	3	4	5	6	7

Neurone F

Connecte tes neurones !







Neurone A



Neurone D



Neurone B



Neurone E



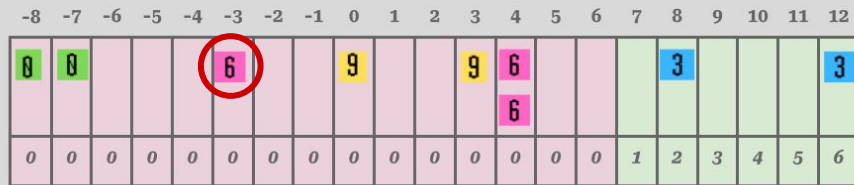
Neurone C



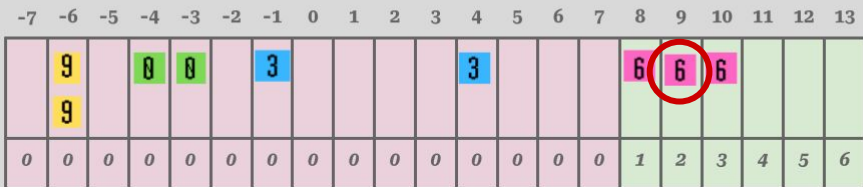
Neurone F



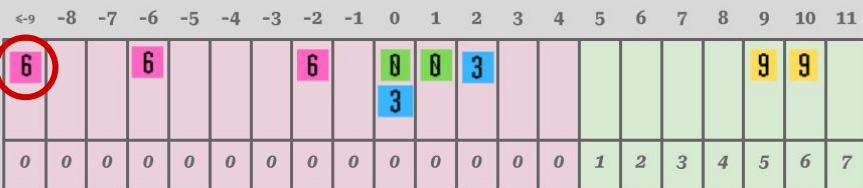
Neurone vert



Neurone bleu



Neurone rose



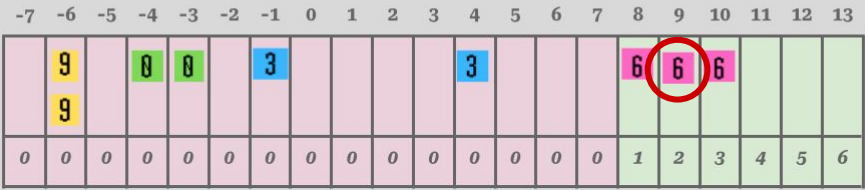
Neurone jaune



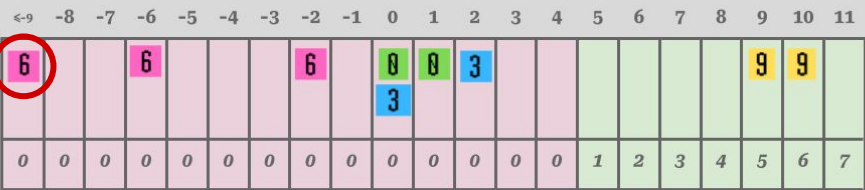
Neurone vert



Neurone bleu



Neurone rose



Neurone jaune







<-8	-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7	8	9	10	11	12
3	3			6		9		9							6		0			0
0	0	0	0	6	0	0	0	0	0	0	0	0	0	0	0	1	2	3	4	5

Neurone vert



-8	-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7	8	9	10	11	12	
0	0			6		9		9		6						3				3	
0	0	0	0	0	0	0	0	0	0	0	0	6	0	0	0	1	2	3	4	5	6

Neurone bleu



-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7	8	9	10	11	12	13
	9		0	0		3					3				6	6	6			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	3	4	5	6

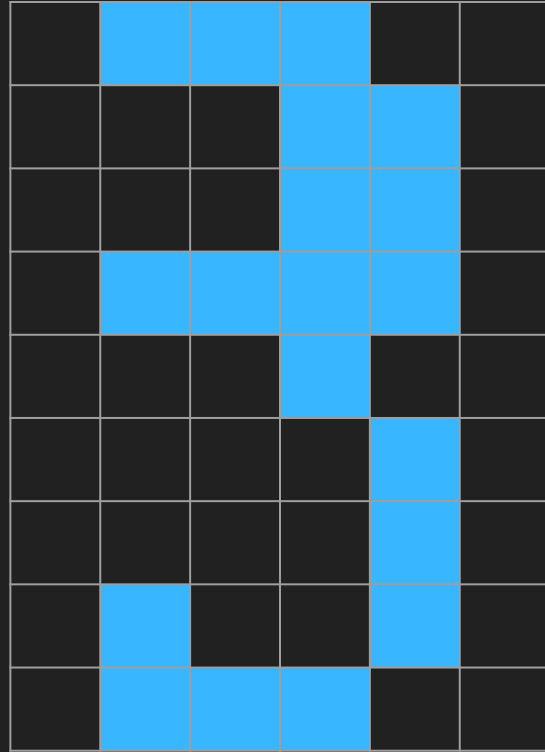
Neurone rose



<-9	-8	-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7	8	9	10	11	
6			6				6		0	0	3							9	9		
0	0	0	0	0	0	0	0	0	0	0	3	0	0	0	1	2	3	4	5	6	7

Neurone jaune





3	4	5	6	7	8	9	10	11	12	13	14	15
		6		0	6			9	3			
				0	6			3	3			
0	0	0	0	0	0	1	2	3	4	5	6	7

Neurone A

3	4	5	6	7	8	9	10	11	12	13	14	15
		0	0		3		3		6	3		
		9	9				6		6			
0	0	0	0	0	1	2	3	4	5	6	7	8

Neurone D

1	2	3	4	5	6	7	8	9	10	11	12	13
		0			0		3	3	6			
		6						6	9			
								9	9			
0	0	0	0	0	0	0	1	2	3	4	5	6

Neurone B

12	13	14	15	16	17	18	19	20	21	22	23	24
3	3	9		9		6	0	0				6
				3			6					
0	0	0	0	0	1	2	3	4	5	6	7	8

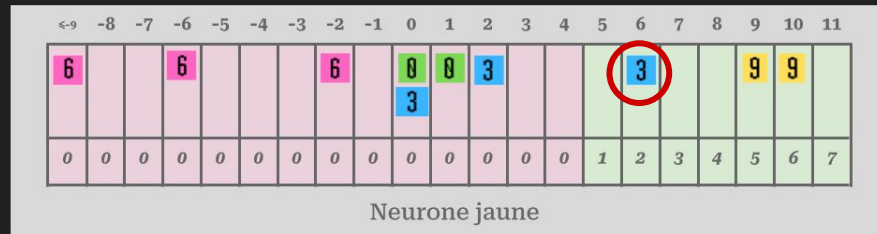
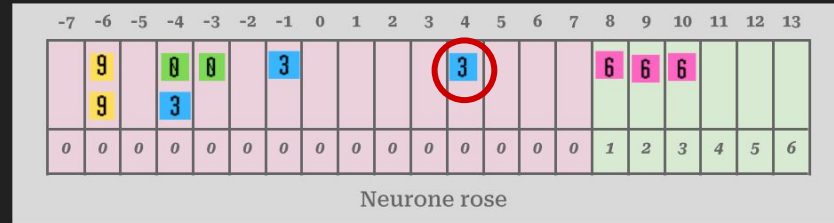
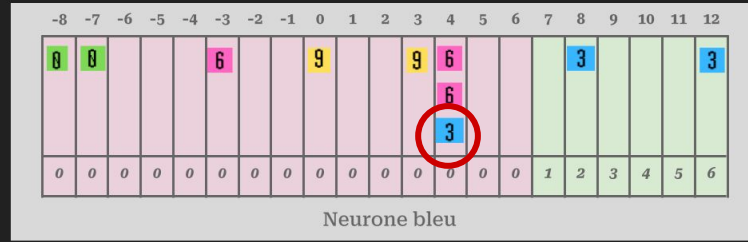
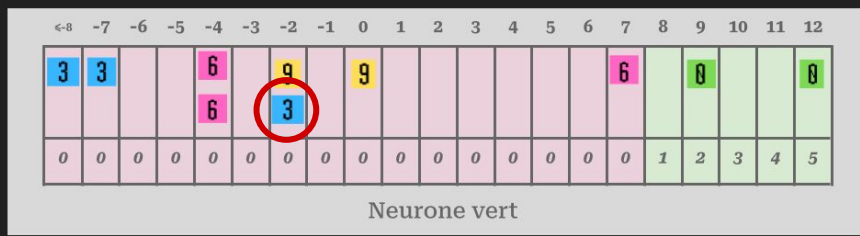
Neurone E

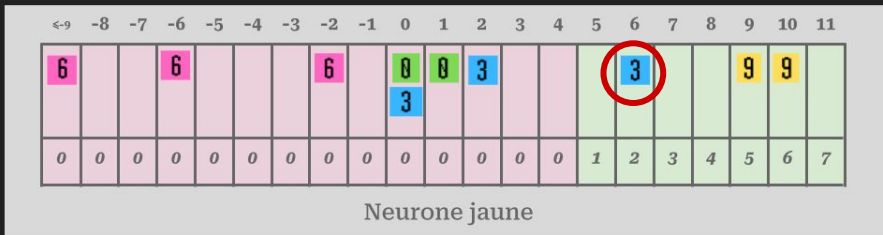
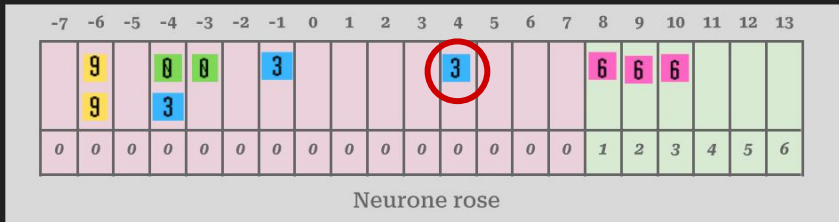
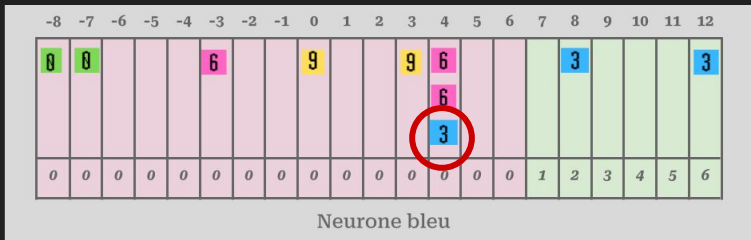
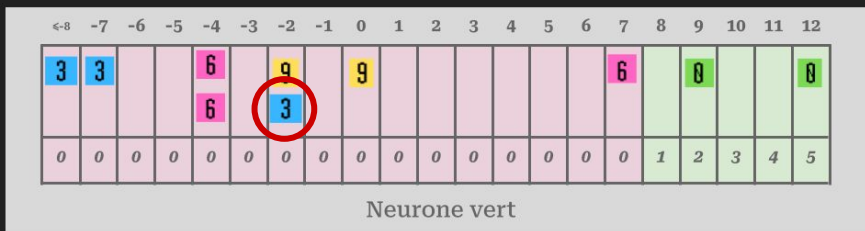
11	12	13	14	15	16	17	18	19	20	21	22	23
3				3	6	6		3	9	0	9	
				6						0		
0	0	0	0	0	0	0	1	2	3	4	5	6

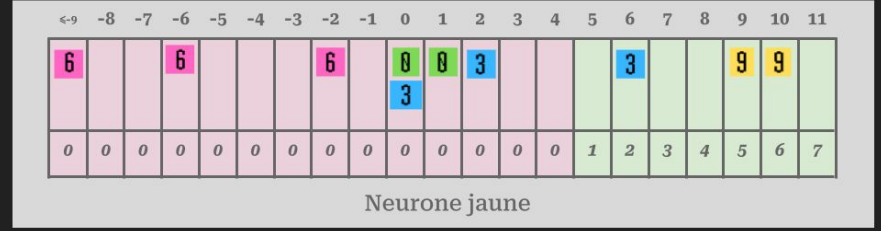
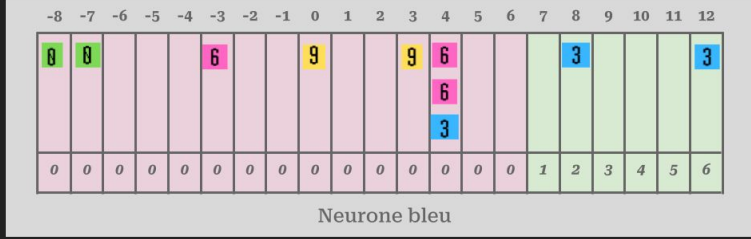
Neurone C

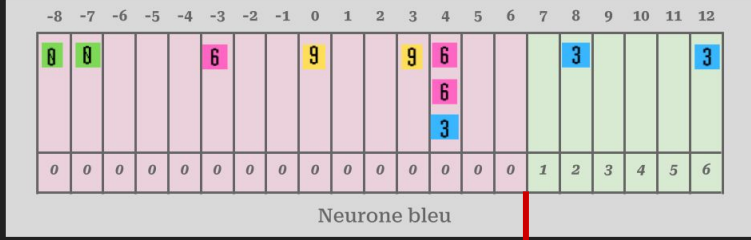
0	1	2	3	4	5	6	7	8	9	10	11	12
				3	9	3	0		0			
				6		9	3		6			
0	0	0	0	0	0	1	2	3	4	5	6	7

Neurone F

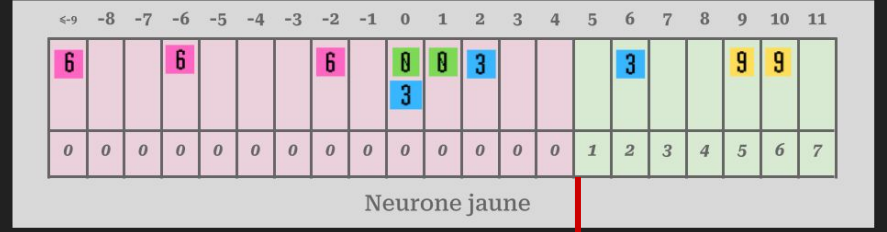
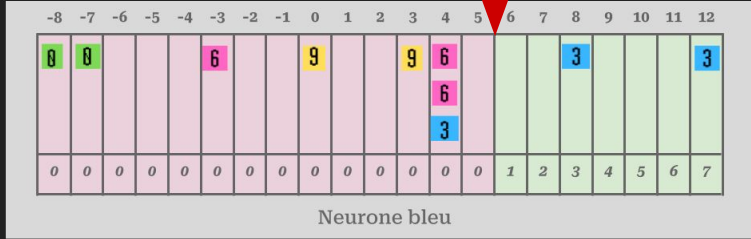




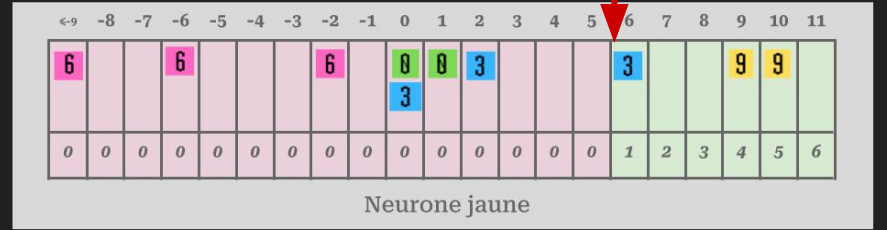


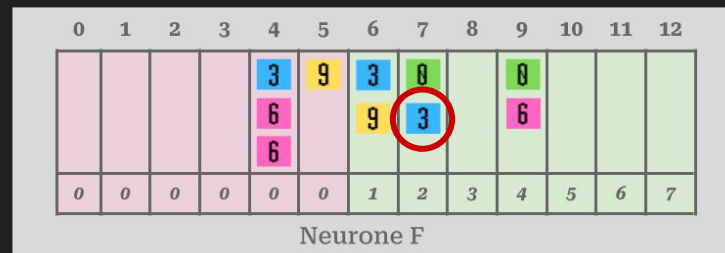
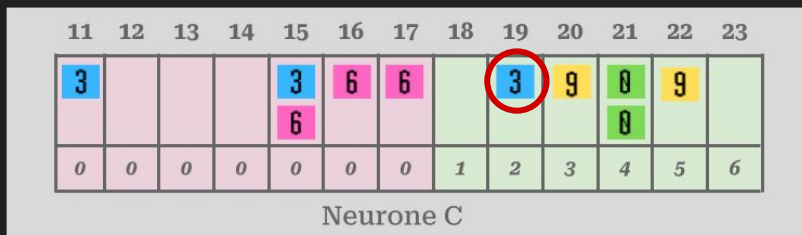
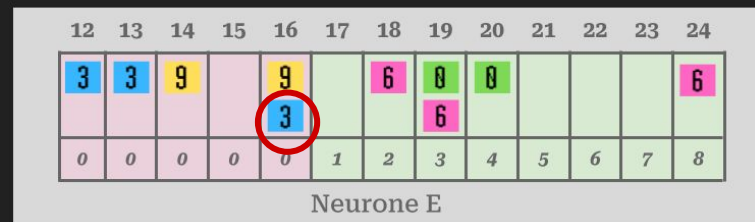
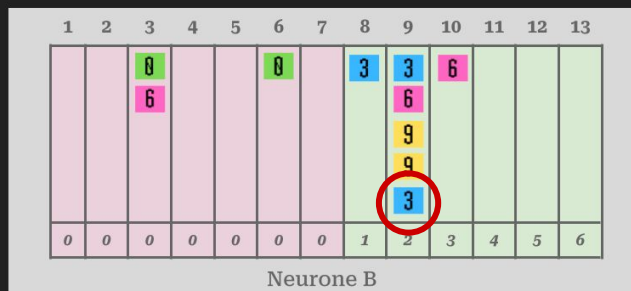
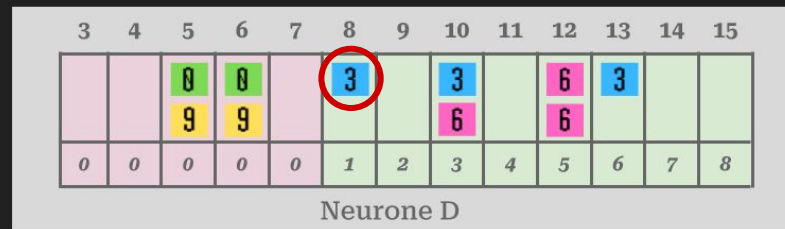
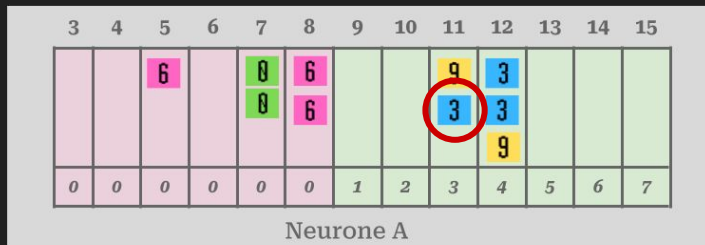


-1



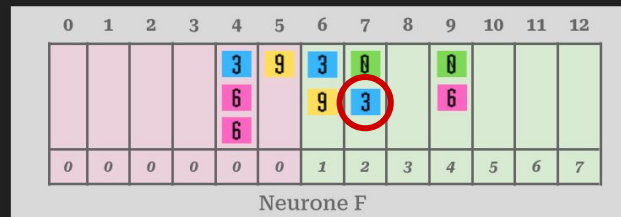
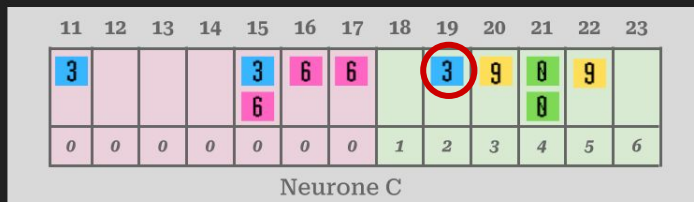
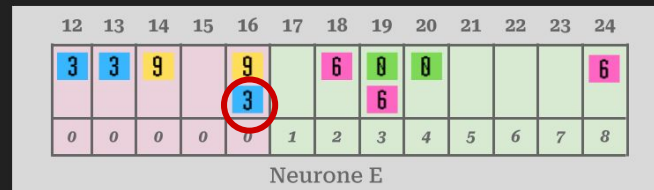
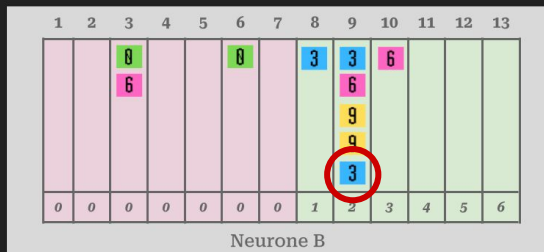
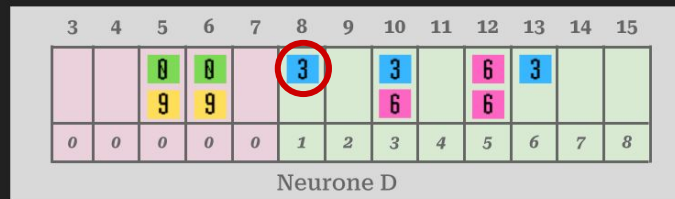
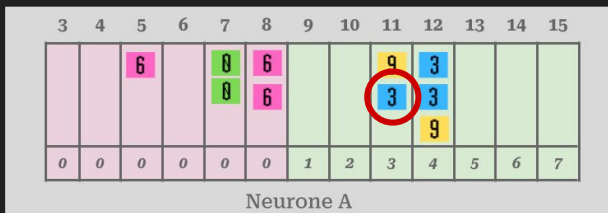
+1





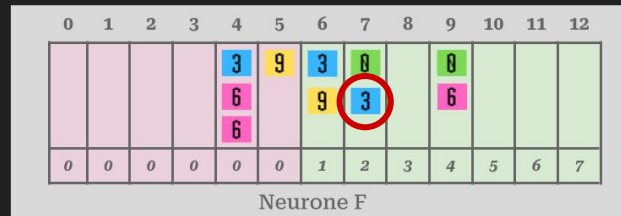
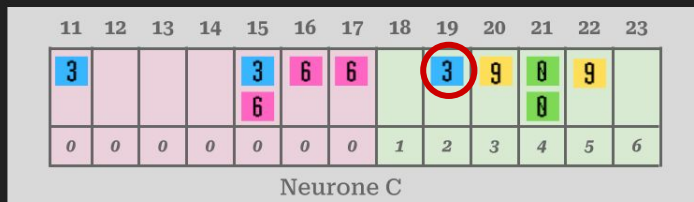
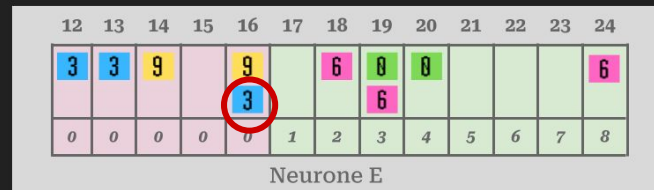
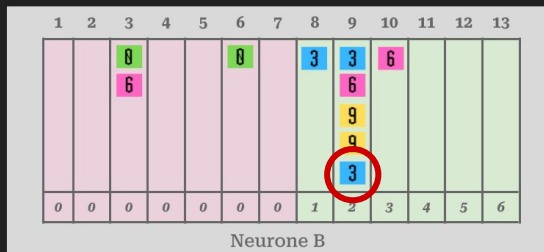
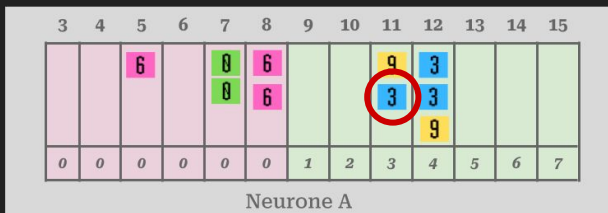
Neurone bleu : $A + B + D - C - E$

Neurone jaune : $A + B + C - D - E$



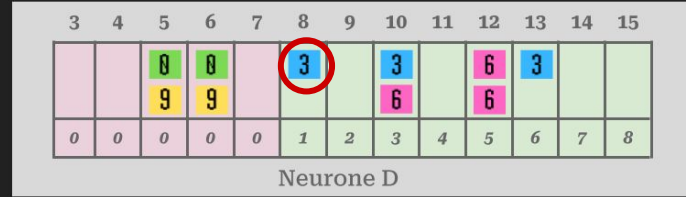
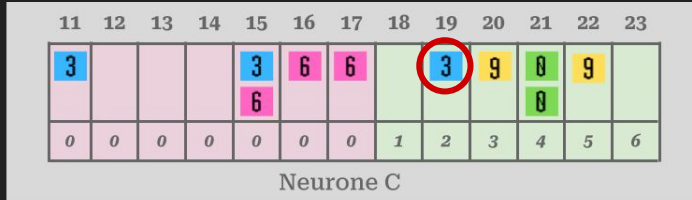
Neurone bleu : $A + B + D - C - E$

Neurone jaune : $A + B + C - D - E$



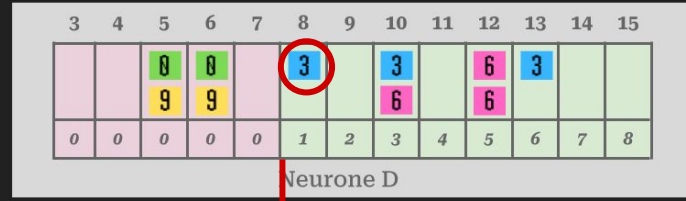
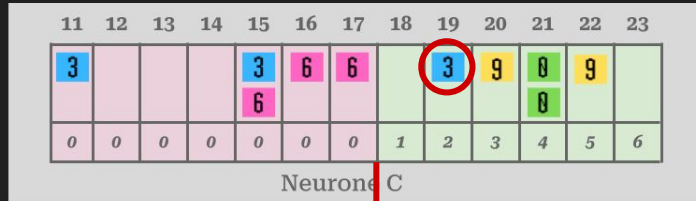
Neurone bleu : $A + B + D - C - E$

Neurone jaune : $A + B + C - D - E$

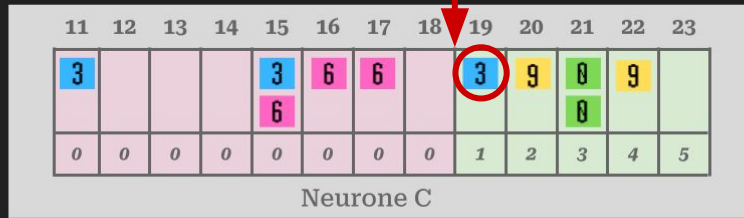


Neurone bleu : $A + B + \boxed{D - C} - E$

Neurone jaune : $A + B + \boxed{C - D} - E$

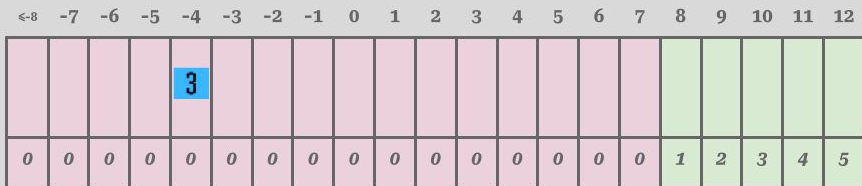


+1

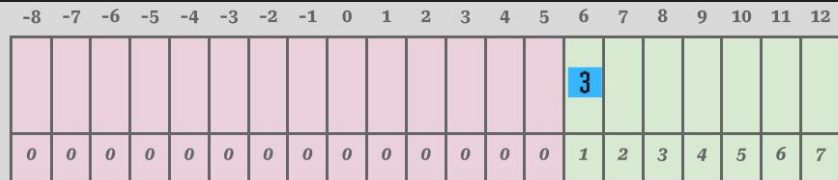


-1

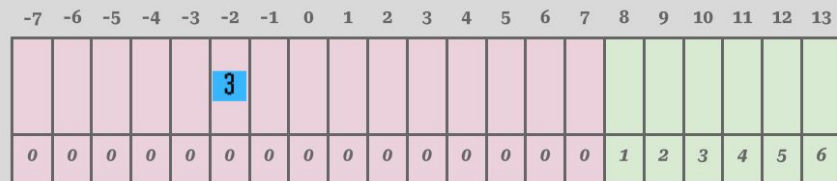




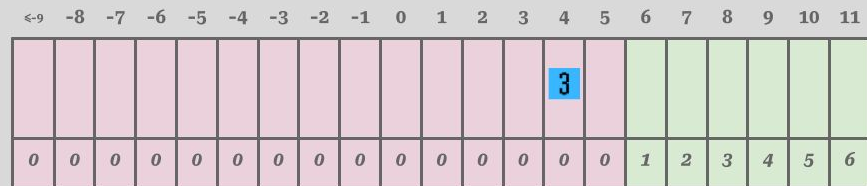
Neurone vert



Neurone bleu

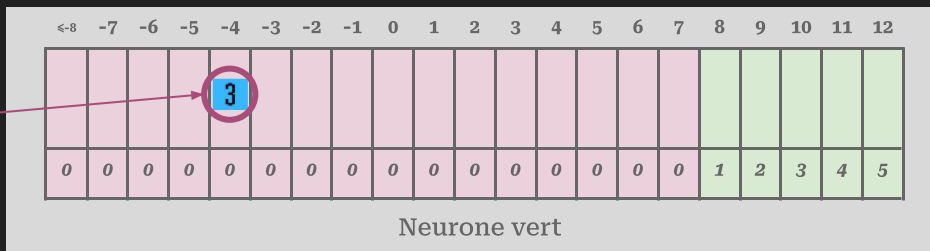


Neurone rose

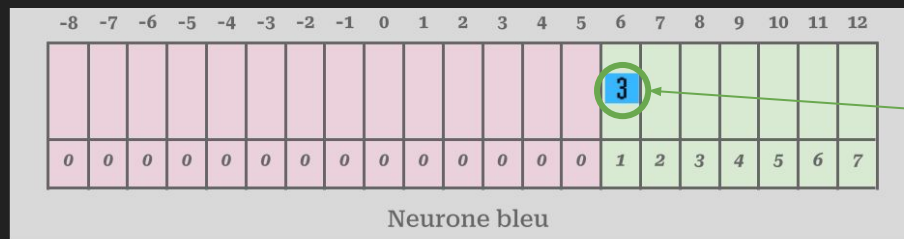


Neurone jaune

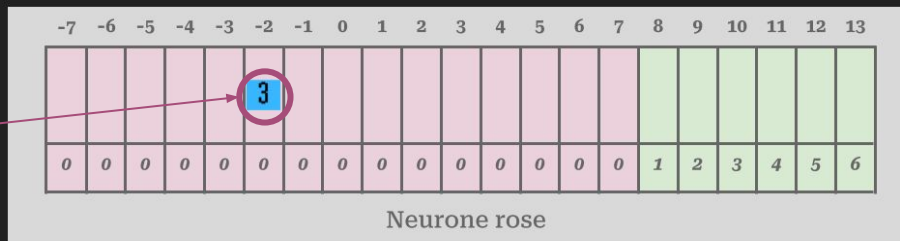
CE N'EST PAS UN 0



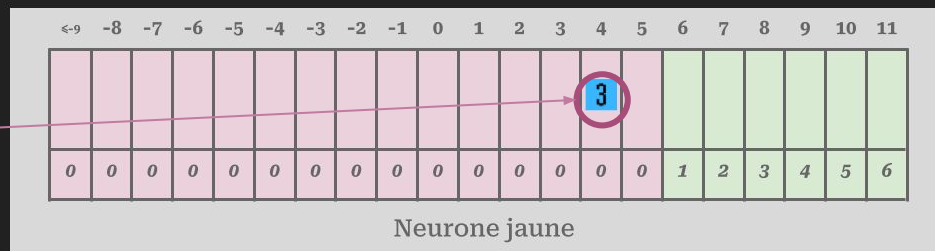
C'EST UN 3

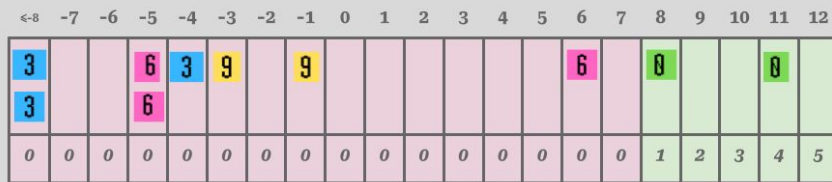


CE N'EST PAS UN 6

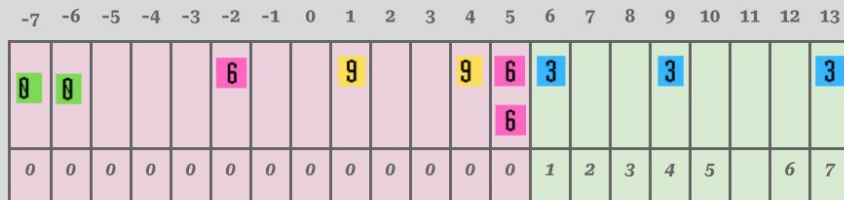


CE N'EST PAS UN 9





Neurone vert



Neurone bleu

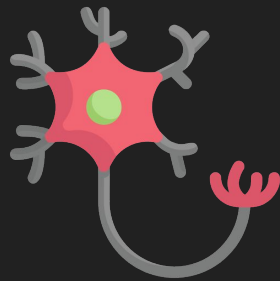


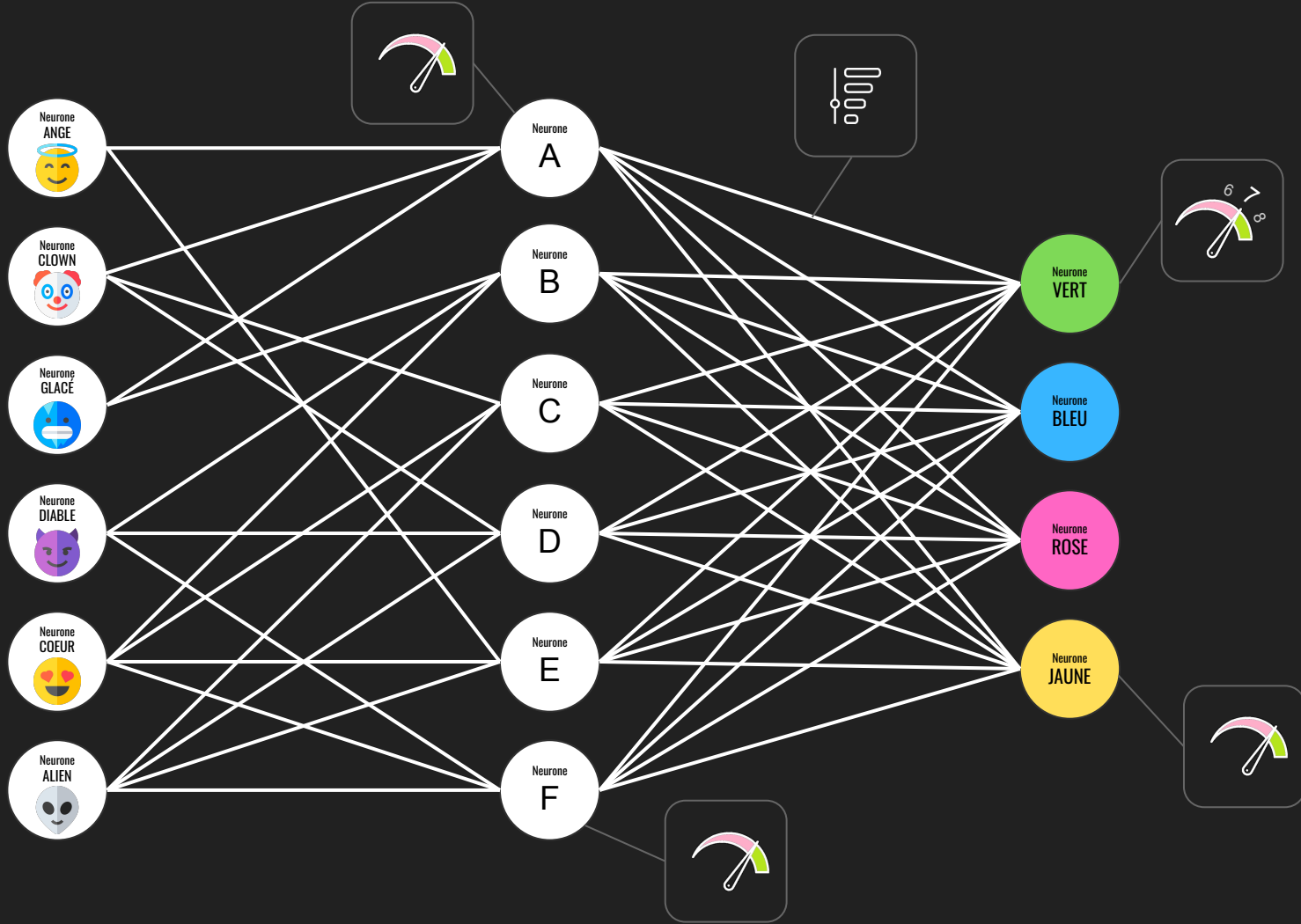
Neurone rose



Neurone jaune

Connecte tes neurones !



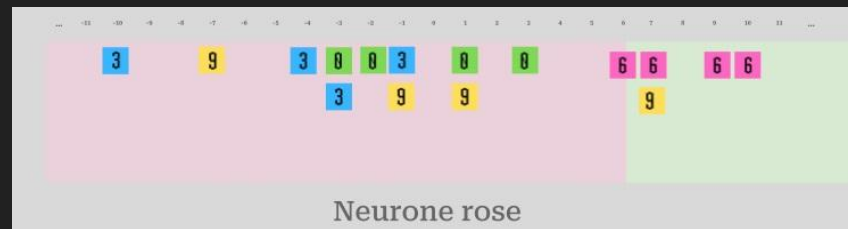


Le réseau et son apprentissage en Python

Le réseau et son apprentissage en Python

```
10 import numpy as np
11
12
13
14 sortie_cachee=np.empty((16,6),dtype='float64')
15 sortie_finale=np.empty((16,4),dtype='float64')
16 seuil_cache=np.empty((6, ),dtype='float64')
17 seuil_final=np.empty((4, ),dtype='float64')
18 erreur=np.empty((16,6),dtype='float64')
19
20 ##### INITIALISATION DES POIDS ET DES SEUILS #####
21
22 W=np.empty((6,6),dtype='float64')
23 W[0]=[-1,1,1,0,0,0]
24 W[1]=[1,1,0,0,0,-1]
25 W[2]=[0,0,1,1,1,0]
26 W[3]=[0,1,0,-1,0,1]
27 W[4]=[1,0,0,0,1,1]
28 W[5]=[0,0,0,1,-1,1]
29
30 masque=np.empty((6,6))
31
32 masque[0]=[1,1,1,0,0,0]
33 masque[1]=[1,1,0,0,0,1]
34 masque[2]=[0,0,1,1,1,0]
35 masque[3]=[0,1,0,1,0,1]
36 masque[4]=[1,0,0,0,1,1]
37 masque[5]=[0,0,0,1,1,1]
38
39 seuil_cache=np.array([8,7,18,6,16,5],dtype='float64')
40
41 P=np.empty((4,6),dtype='float64')
42 P[0]=[-1,-1,1,-1,1,1]
43 P[1]=[1,1,-1,1,-1,0]
44 P[2]=[-1,1,-1,1,1,-1]
45 P[3]=[1,1,1,-1,-1,0]
46
47 seuil_final=np.array([7,5,6,5],dtype='float64')
48
49 ##### LES DONNEES #####
50
51 test=np.empty((16,6),dtype='float64')
52
53 test[0]=[7,7,7,8,6,7]
54 test[1]=[6,4,9,6,6,7]
55 test[2]=[7,4,7,6,6,6]
56 test[3]=[4,5,8,5,7,5]
57 test[4]=[2,9,5,5,5,6]
58 test[5]=[1,10,3,3,5,6]
59 test[6]=[4,9,6,7,6,6]
60 test[7]=[2,8,8,7,5,6]
61 test[8]=[5,9,4,5,7,6]
62 test[9]=[5,9,4,4,7,7]
63 test[10]=[8,7,6,5,6,10]
64 test[11]=[4,9,6,4,8,7]
65 test[12]=[3,8,7,7,6,5]
66 test[13]=[4,7,8,7,7,5]
67 test[14]=[4,7,7,5,6,7]
68 test[15]=[5,6,7,6,7,5]
69
70 label = np.array([0,0,0,1,1,1,1,2,2,2,3,3,3,3])
71
72
73 ##### PARAMETRES DE L'APPRENTISSAGE #####
74
75
76 pas = 0.0001 #le pas dans le flot gradient
77 coef = 0.7 #coef dans la fonction de coût d'erreur qui est une fonction exponentielle
78
79 ##### L'APPRENTISSAGE PAR RETROPROPAGATION DU GRADIENT #####
80
81 # fonction de coût
82 def cout(y,l,a):
83     s = np.where(np.arange(4)[np.newaxis,:]==l[: ,np.newaxis],-1,1)
84     return np.exp(a*s*y)
85
86 # dérivée de la fonction de coût
87 def dercout(y,l,a):
88     s = np.where(np.arange(4)[np.newaxis,:]==l[: ,np.newaxis],-1,1)
89     return a*s*np.exp(a*s*y)
90
91 for epoque in range(100001):
92     ###calcul des sorties (passage forward)
93     # calcul de l'activité de la couche cachée par produit scalaire
94     # (i.e. somme pondérée) avec les entrées et ...
95     sortie_cachee = np.dot(test,W.T)-seuil_cache
96     # ... passage par la fonction d'activation ReLU
97     sortie_cachee = np.maximum(0,sortie_cachee)
98     # calcul de la sortie du réseau par produit scalaire avec la couche cachée
99     sortie_finale = np.dot(sortie_cachee,P.T)-seuil_final
100     # calcul de l'erreur du réseau
101     erreur = cout(sortie_finale,label,coef)
102     ### fin du calcul des sorties ###
103     #### ajustement des seuils et des poids ####
104     #### ajustement des seuils finaux ####
105     # gradient de la couche de sortie
106     grad = dercout(sortie_finale,label,coef)
107     # mise à jour du seuil de la couche de sortie
108     seuil_final += 10*pas*np.sum(grad,axis=0)
109     # mise à jour des poids de la couche de sortie
110     P -= pas*np.dot(grad.T,sortie_cachee)
111     # rétropropagation du gradient à la couche cachée
112     grad_cache = np.dot(grad,P)*(sortie_cachee!=0) #sortie_cachee!=0 (dérivée de ReLU)
113     # mise à jour du seuil de la couche cachée
114     seuil_cache += pas*np.sum(grad_cache,axis=0)
115     # mise à jour des poids de la couche cachée
116     W -= pas*np.dot(grad_cache.T,test)
117     W *= masque # on force les connexions inexistantes à 0
118
119
120     ###calcul des sorties au final (passage forward)
121     sortie_cachee = np.dot(test,W.T)-seuil_cache[np.newaxis,:]
122     sortie_cachee = np.maximum(0,sortie_cachee)
123     sortie_finale = np.dot(sortie_cachee,P.T)-seuil_final[np.newaxis,:]
124     erreur = cout(sortie_finale,label,coef)
125
```

Avec quelques exemples en plus



Après 100 itérations



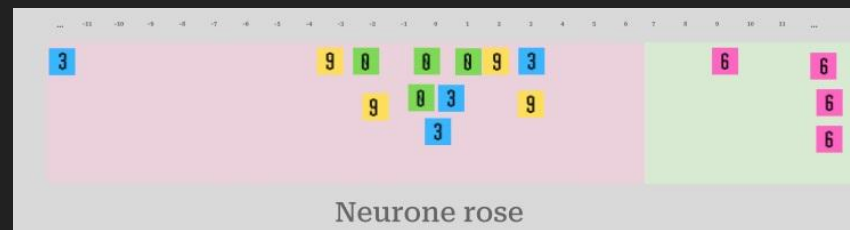
Après 1000 itérations



Après 5000 itérations



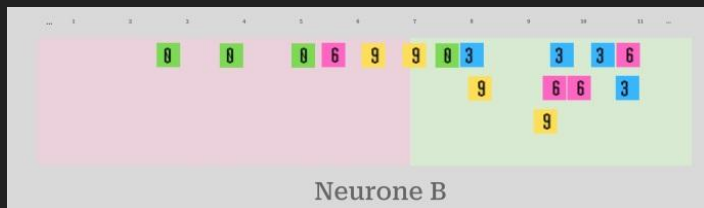
Après 20000 itérations



Après 50000 itérations



Après 50000 itérations



Neurone bleu

$$2A + 1,2B - 1,1C + 0,5D - 2,7E + 3F$$

Neurone E

$$0,7 \text{ 😇} + 1,2 \text{ 😍} + \text{ 👁}$$